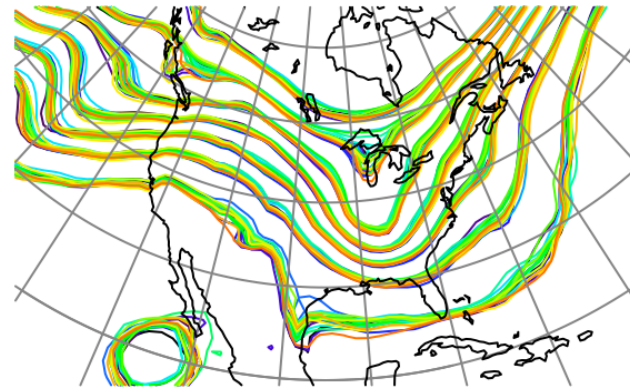


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## DART\_LAB Tutorial Section 3: Sampling error and localization.



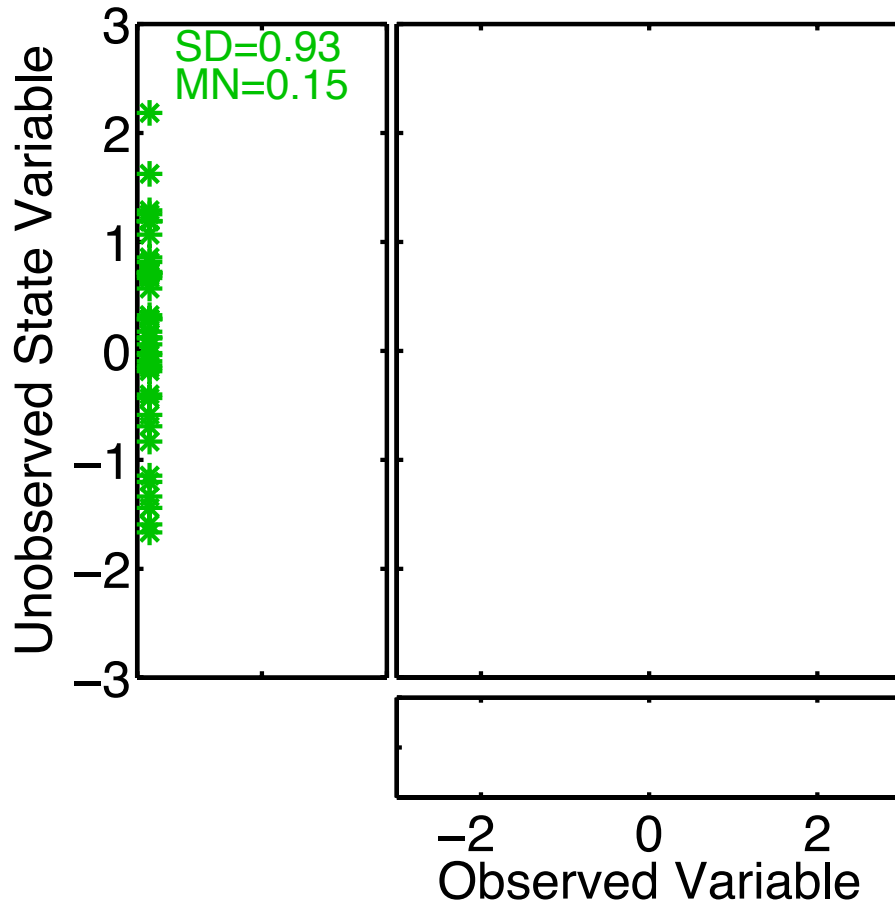
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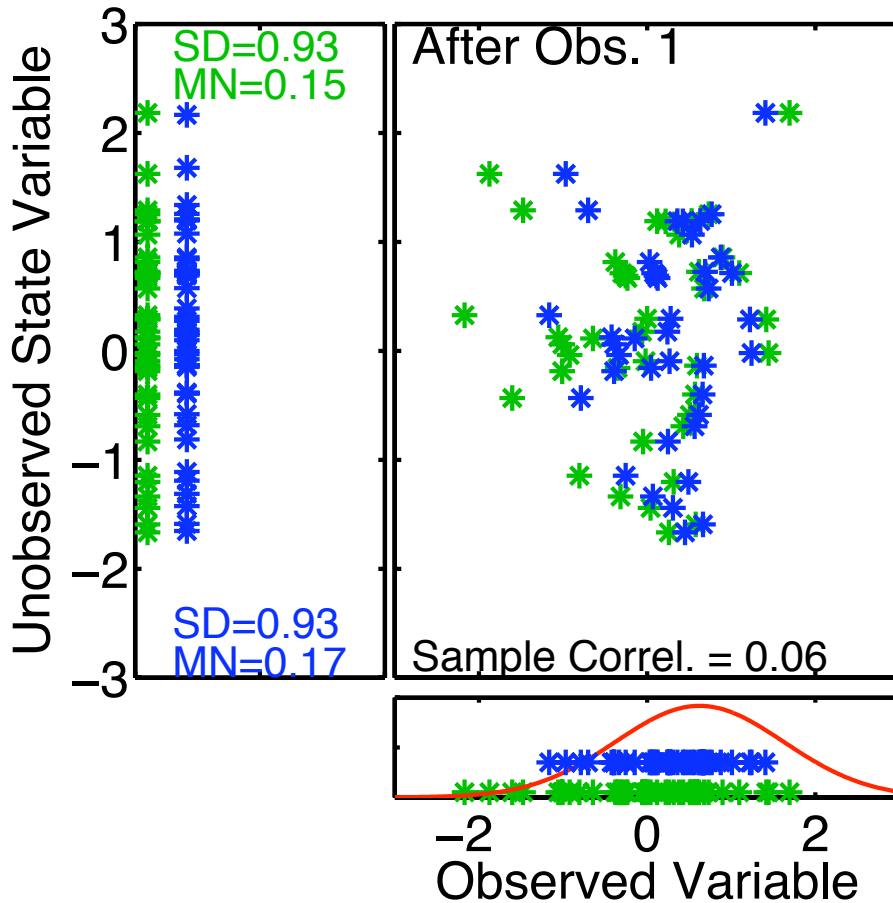
# Regression Sampling Error



Suppose unobserved state variable is known to be unrelated to observed variables.

Unobserved variable **should remain unchanged**.

# Regression Sampling Error

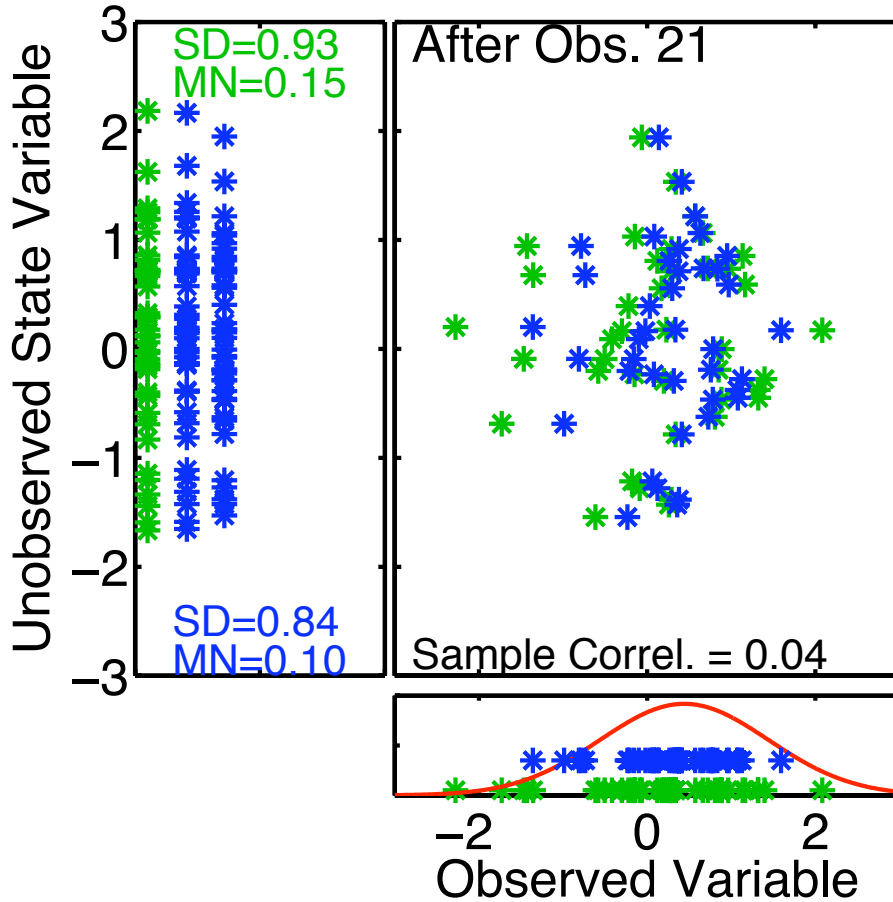


Suppose unobserved state variable is known to be unrelated to observed variables.

Finite samples from joint distribution have non-zero correlation, expected  $|\text{corr}| = 0.19$  for 20 samples.

After one observation, unobserved variable mean and standard deviation change.

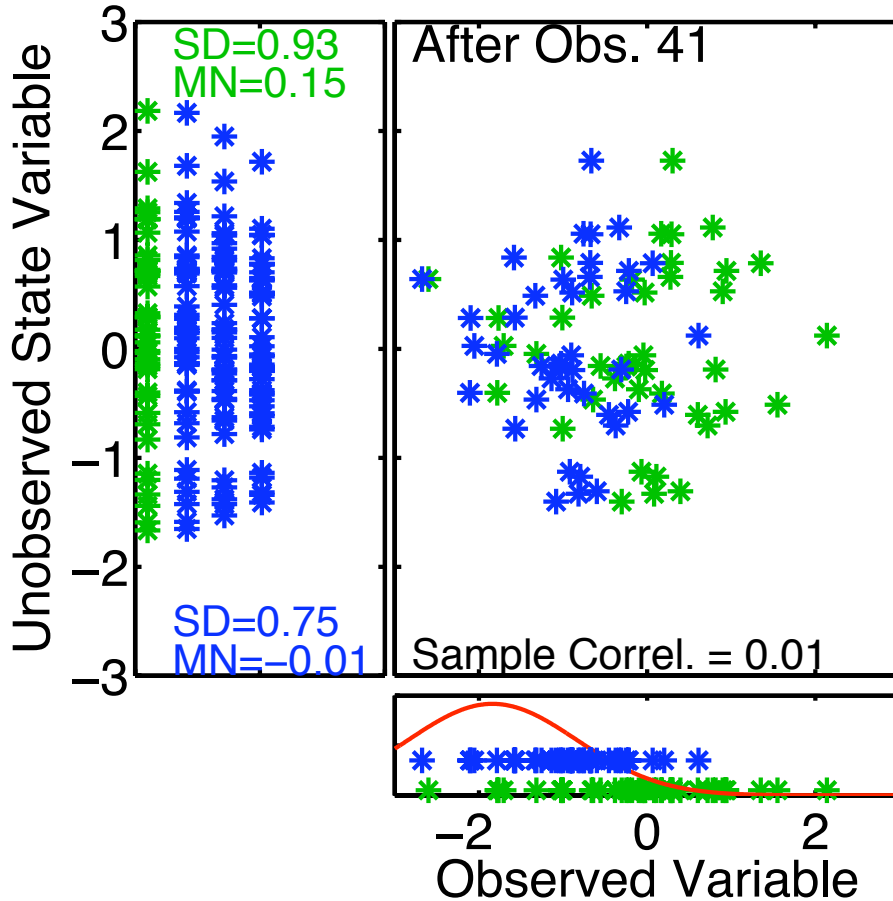
# Regression Sampling Error



Suppose unobserved state variable is known to be unrelated to observed variables.

Unobserved mean follows a random walk as more observations are used.

# Regression Sampling Error

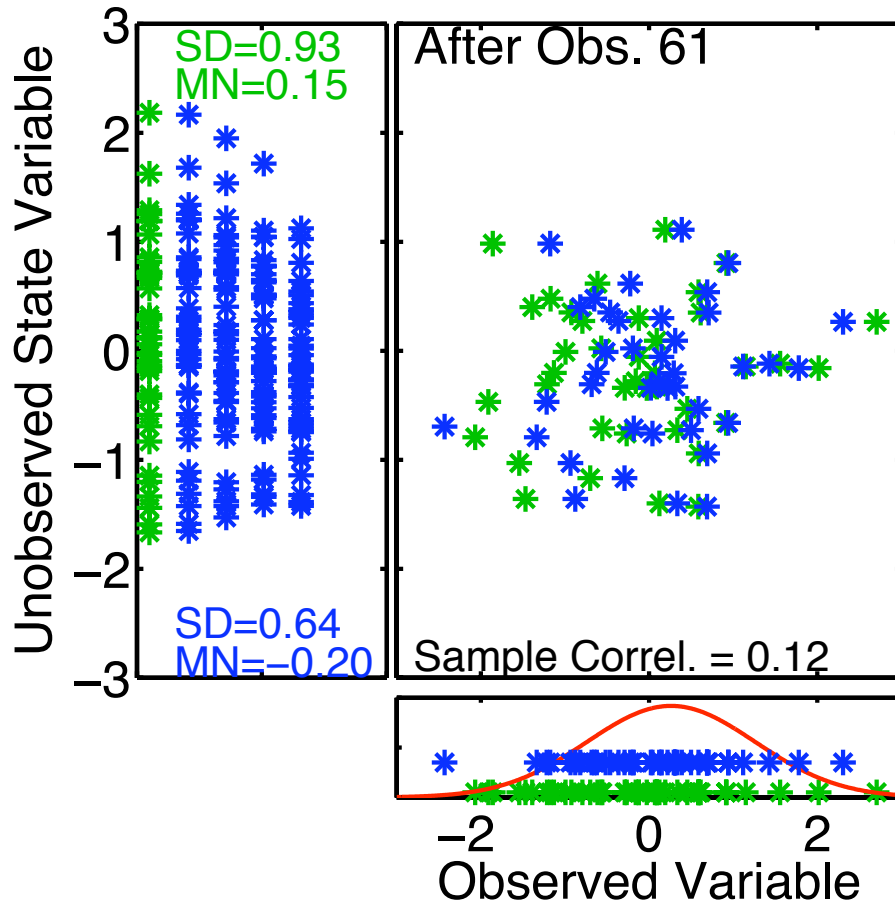


Suppose unobserved state variable is known to be unrelated to observed variables.

Unobserved mean follows a random walk as more observations are used.

Unobserved standard deviation consistently decreases.

# Regression Sampling Error

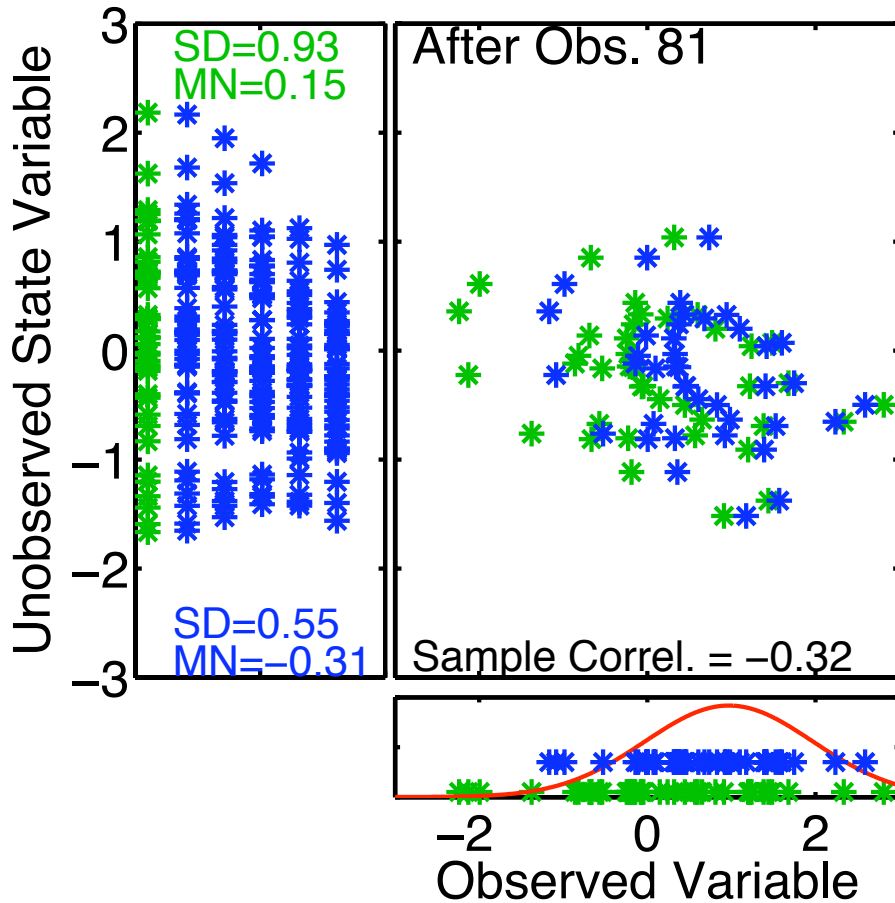


Suppose unobserved state variable is known to be unrelated to observed variables.

Unobserved mean follows a random walk as more observations are used.

Unobserved standard deviation consistently decreases.

# Regression Sampling Error

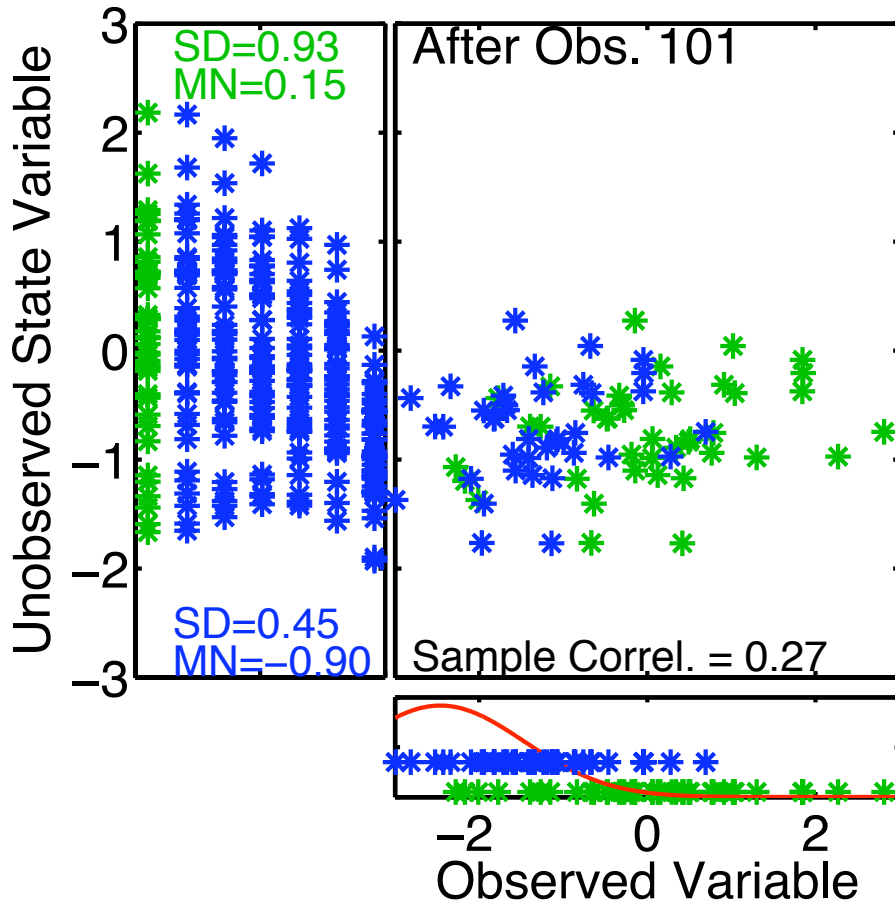


Suppose unobserved state variable is known to be unrelated to observed variables.

Unobserved mean follows a random walk as more observations are used.

Unobserved standard deviation consistently decreases.

# Regression Sampling Error



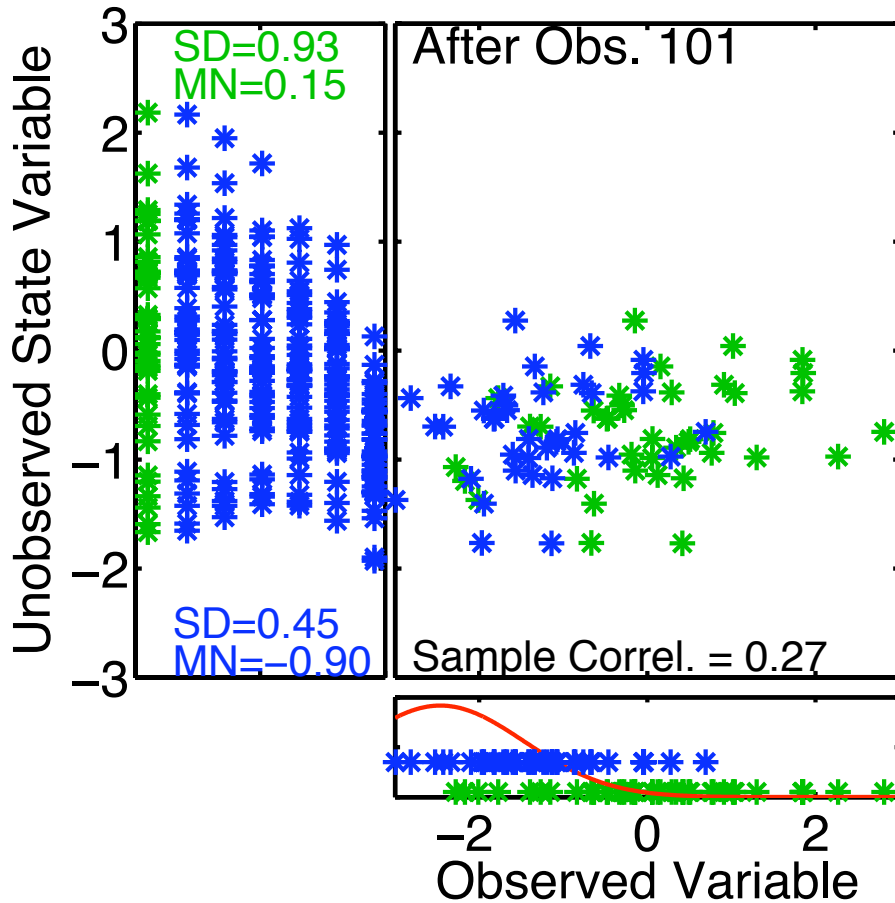
Suppose unobserved state variable is known to be unrelated to observed variables.

Unobserved mean follows a random walk as more observations are used.

Unobserved standard deviation consistently decreases.



# Regression Sampling Error



Suppose unobserved state variable is known to be unrelated to observed variables.

- Estimates of unobserved are too confident.
- Give less weight to subsequent meaningful observations.
- Meaningful observations can end up being ignored.

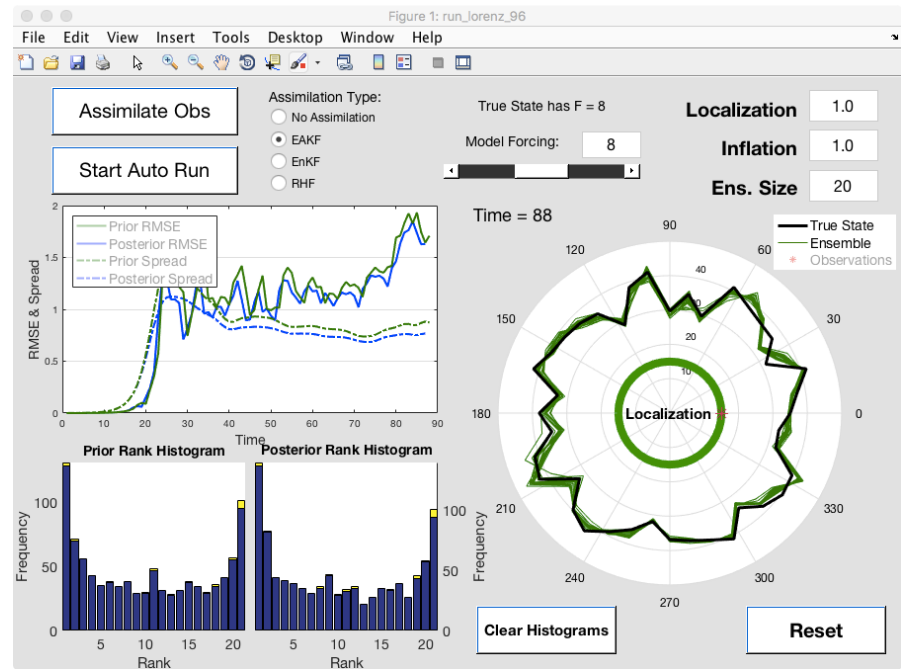
# Regression Sampling Error

Ignoring meaningful observations due to insufficient spread is one form of filter divergence.

This could be seen in the Lorenz-96 assimilation example from the end of DART\_LAB Section 2.

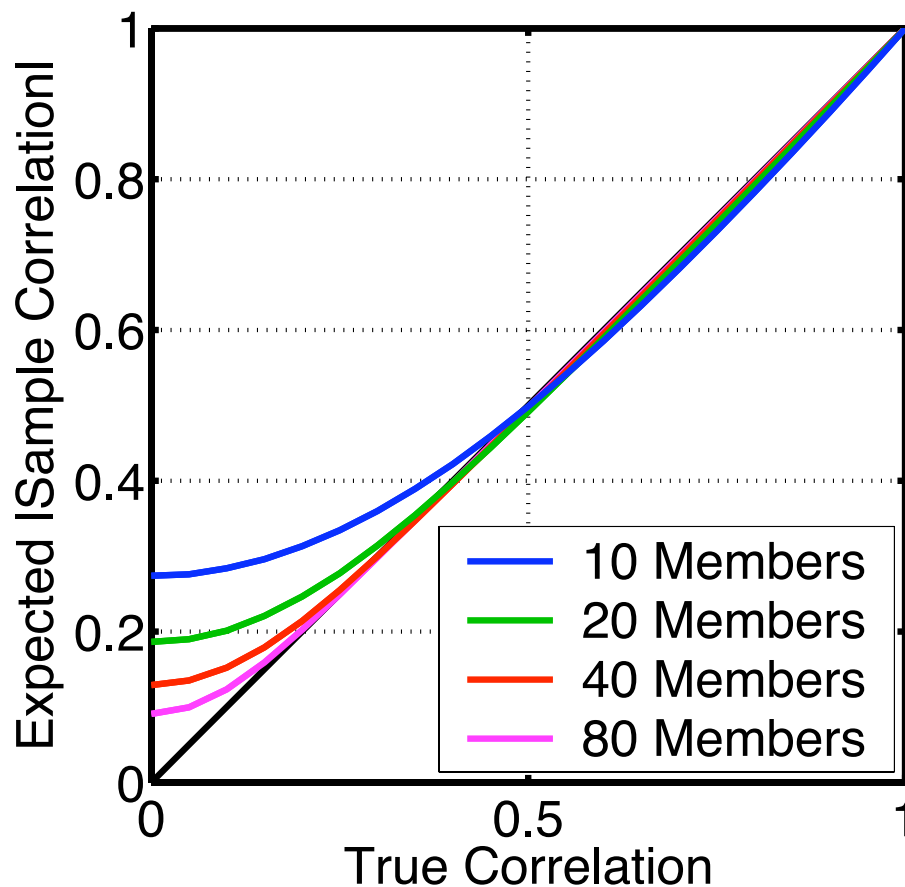
Spread became small, filter thinks it has good estimate.

Error was large because good observations were ignored.



Look how often the truth was outside the ensemble!

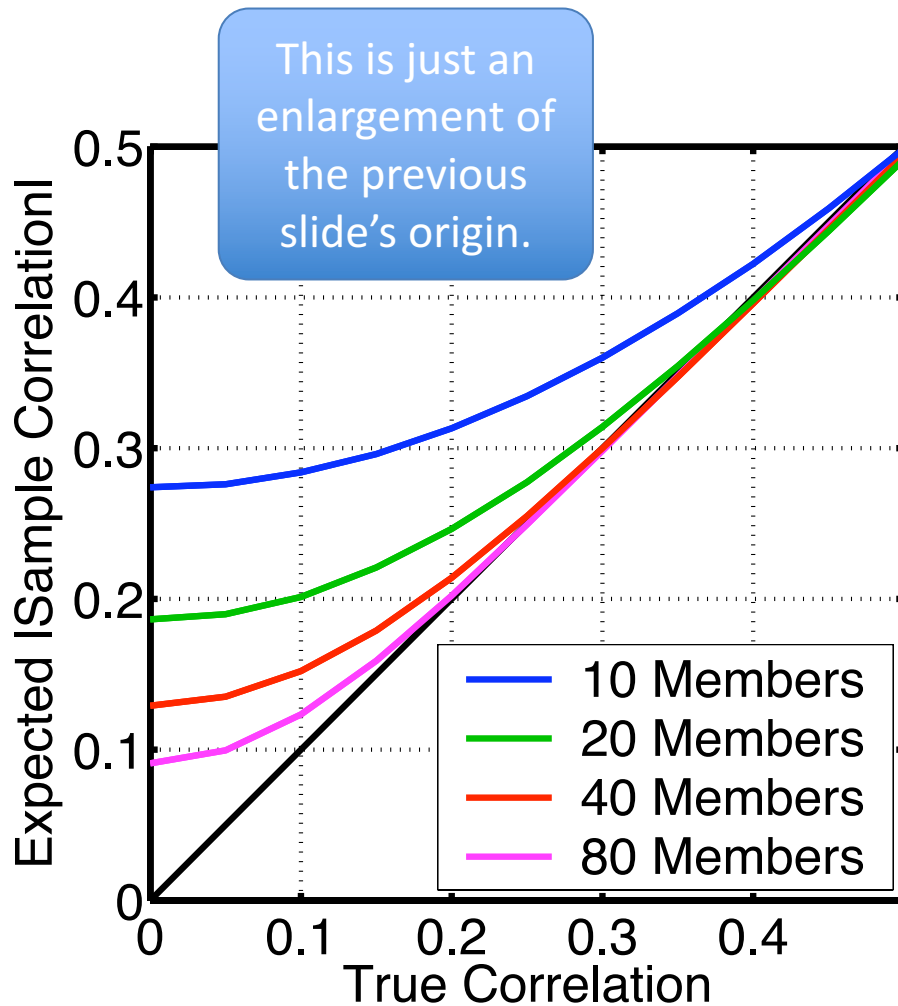
# Regression Sampling Error



Absolute value of expected sample correlation vs. true correlation.

Errors decrease for large ensembles and for correlations with absolute value close to 1.

# Regression Sampling Error



For small true correlations, sampling errors are undesirably large even for 80 members!

# Ways to deal with Regression Sampling Error

1. Ignore it if number of weakly correlated observations is small and there is a way to maintain prior variance. Worked in Lorenz-63.

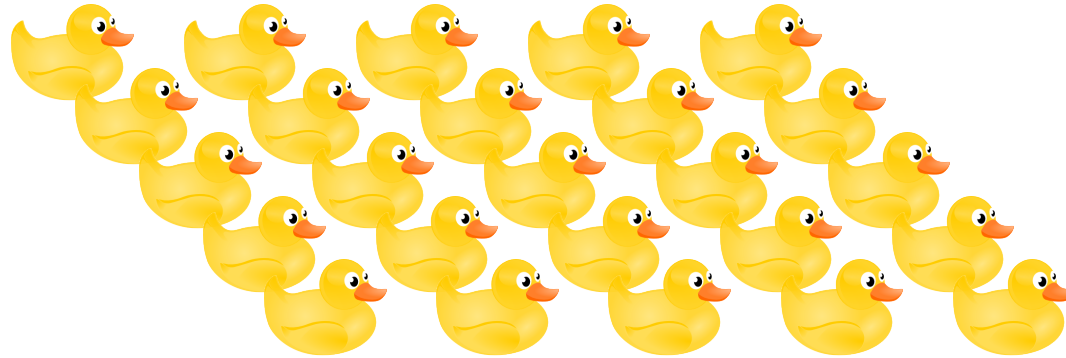


?

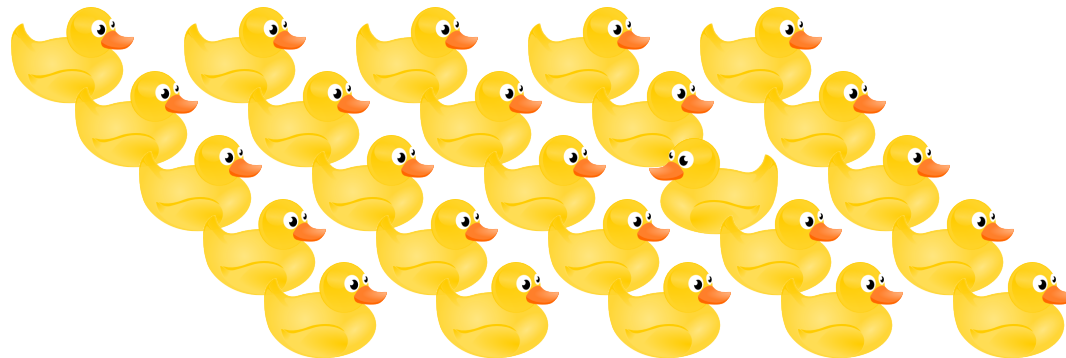


It may work.  
It may not.

# Ways to deal with Regression Sampling Error



2. Use larger ensembles; expensive for large models.

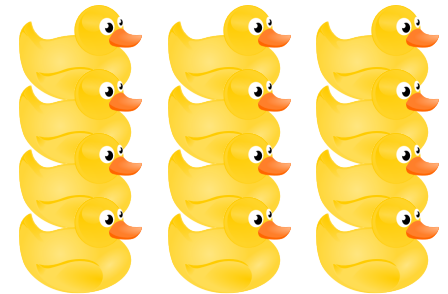


# Ways to deal with Regression Sampling Error

1. Ignore it if number of weakly correlated observations is small and there is a way to maintain prior variance. Worked in Lorenz-63.



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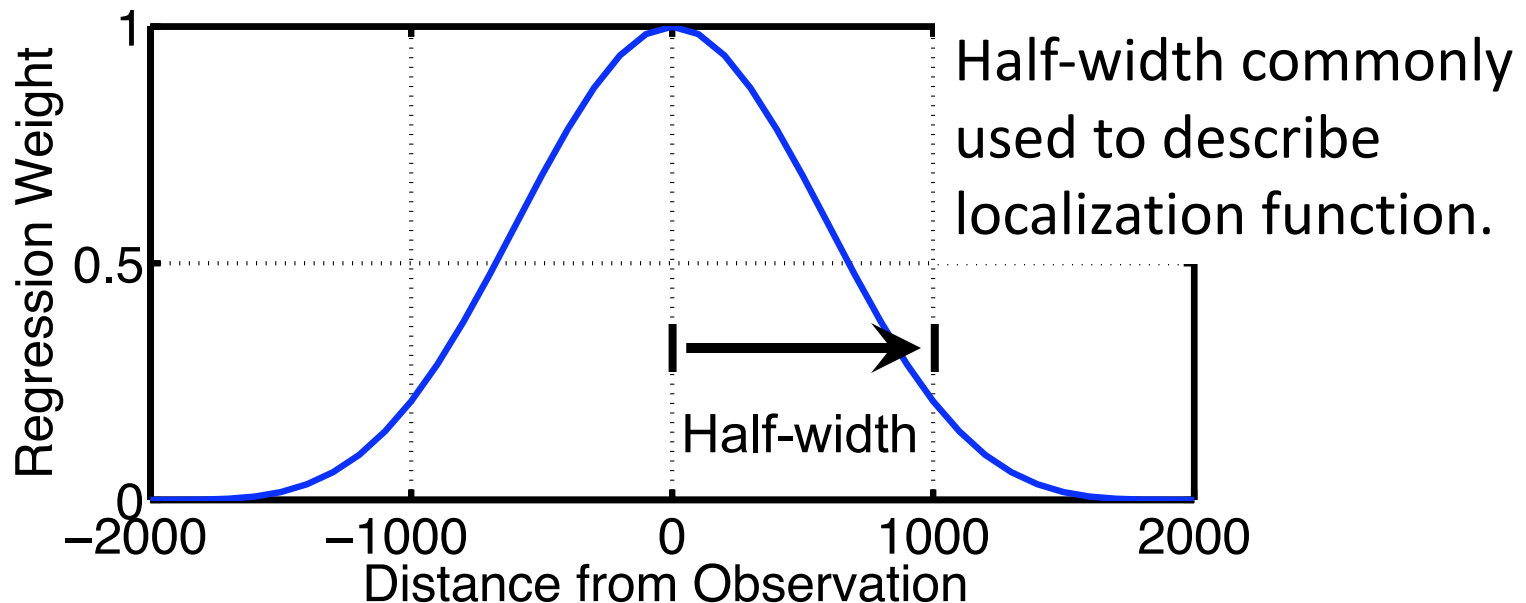
3. Use additional a priori information about relation between observations and state variables.  
*Don't let an observation impact a state variable if they are known to be unrelated.*



# Using additional a priori information: Localization

Try reducing regression factor as function of distance between observation and state variable.

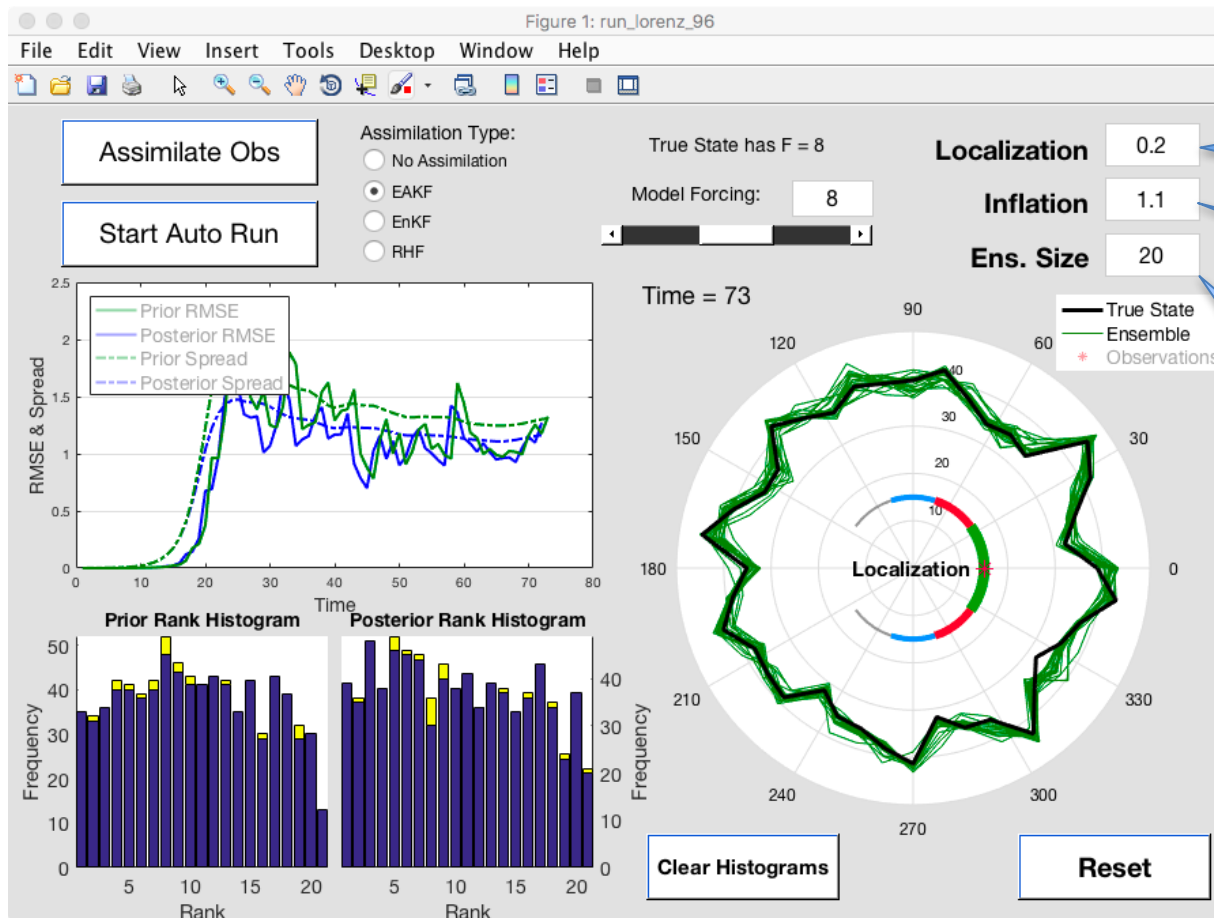
Compactly-supported 5<sup>th</sup> order polynomial (Gaspari-Cohn) is most commonly used for geophysics.





# Matlab Hands-On: run\_lorenz\_96 exercise 2

Purpose: Explore the how localization, ensemble size, and inflation impact Lorenz-96 assimilation.



Choose a Localization.  
Units are fraction of domain.

Choose an Inflation.

Choose an ensemble size.

# Matlab Hands-On: run\_lorenz\_96 exercise 2

## Explore!

- Do an extended free run to see error growth in the ensemble.
- Select EAKF and set localization to 0.2, try an assimilation. Note: the distance around the periodic domain is 1. A 0.2 half-width means no weight is being given to state variables on the opposite side of the domain from an observation.
- Turn the localization off (set it to 1000000) and try a larger ensemble. This may be slow with Matlab; you really need to use the real Fortran DART!
- Try reducing the ensemble size to 10 and varying localization.
- Try adding in some inflation with localization.
- Try selecting model error by changing forcing for the assimilation.

# DART\_LAB Section 3

